
Working with Combined Sewers

Geometric and Hydraulic Elements of Cleveland Egg-Shaped Sewers – Part 1

Kevin L. Enfinger, P.E.

ADS Environmental Services

340 The Bridge Street, Suite 204 | Huntsville, Alabama 35806 | www.adsenv.com/cso

ABSTRACT

Wastewater professionals working with combined sewers often encounter a variety of non-circular sewer cross sections, including egg-shaped sewers. Equations are developed here to calculate the wetted area, wetted perimeter, and surface width for various Cleveland egg-shaped sewers flowing partially full and support a variety of hydraulic calculations.

Part 1 describes the geometry of No. 2 and No. 3 Cleveland egg-shaped sewers, and Part 2 describes the geometry of No. 4 through No. 20. These equations supplant traditional graphical approaches that use geometric and hydraulic elements curves in favor of equations better suited to Smart Sewer applications. The equations are validated and provide a concise reference for those working with egg-shaped sewers in combined sewers located in Cleveland, Ohio.

KEY WORDS

Combined Sewer, Non-Circular Section, Cleveland Egg-Shaped Sewer

Introduction

Combined sewers are designed and constructed with a wide variety of sewer cross sections. While the circular section is most common, other non-circular sections have been used over the years.¹ Working with combined sewers requires an understanding of the geometric and hydraulic elements of these non-circular sections when encountered.

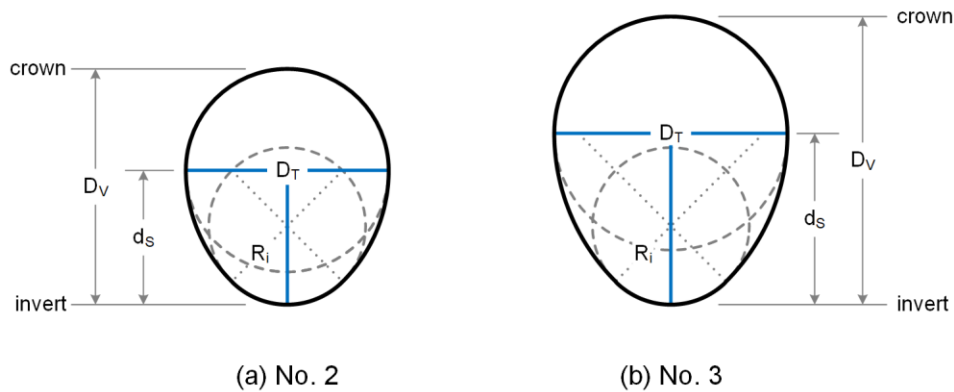
Geometric properties of non-circular sections are found in standard engineering references but are often presented only in graphical form for sewers flowing partially full and where the results are provided as a proportion of values for sewers flowing full.¹ While this approach was sufficient when these sewers were originally designed and constructed, it is insufficient for modern Smart Sewer applications where automated and precise computations are required.

Various egg-shaped sewer sections used in Cleveland, Ohio are the focus of this discussion. Descriptions of No. 2 and No. 3 Cleveland egg-shaped sewers are provided here, and historical perspectives regarding their development and application are presented. The geometric elements of these egg-shaped sections are then defined, and equations for the wetted area, wetted perimeter, and surface width for sewers flowing partially full are provided. The result is a concise reference for wastewater professionals working with egg-shaped sewers in combined sewers located in Cleveland, Ohio.

Description

While various egg-shaped sewers have been developed and used over the years, several unique versions are found in Cleveland, Ohio, two of which are shown in Figure 1. The geometry of these egg-shaped sewers – used for No. 2 and No. 3 Cleveland egg-shaped sewers – begins with the *invert radius* (R_i), and other relevant dimensions – including the transverse diameter (D_T) and vertical diameter (D_V) – are each defined as a function of R_i .

FIGURE 1: Cleveland Egg-Shaped Sewer Cross-Sections



The anatomy of No. 2 and No. 3 Cleveland egg-shaped sewers are shown in Figure 2(a) and Figure 2(b), respectively.

FIGURE 2: Anatomy of a Cleveland Egg-Shaped Sewer

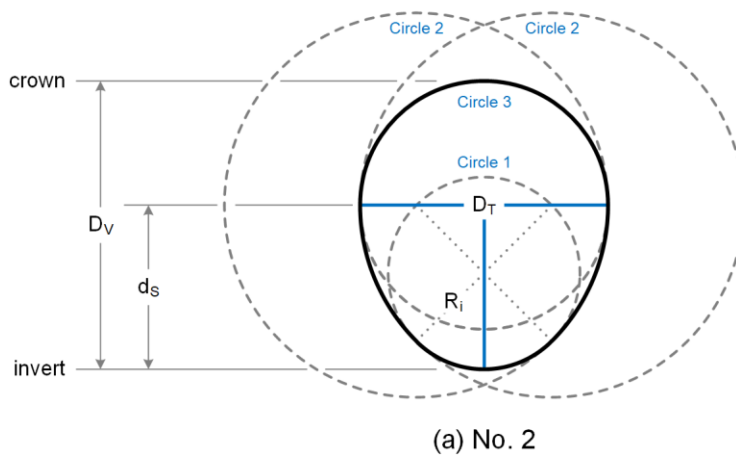
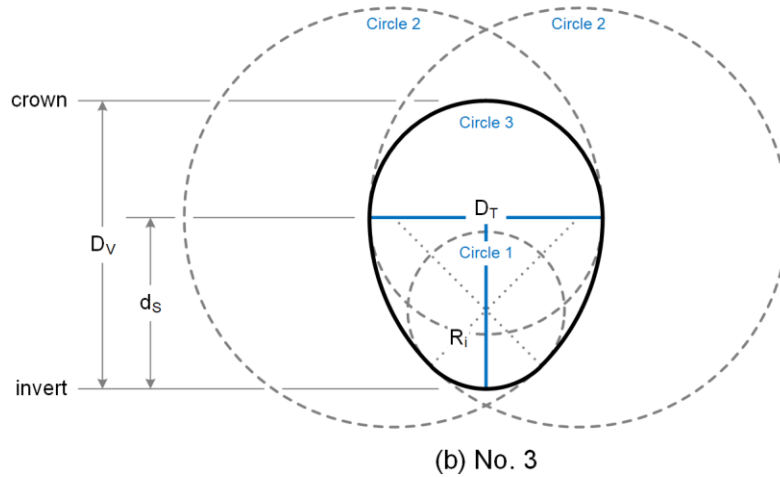


FIGURE 2: Anatomy of a Cleveland Egg-Shaped Sewer



These egg-shaped sewers are compound cross-sections formed by several tangent circles. Circle 1 forms the invert of the egg-shaped sewer, which is positioned at a specified distance (d_s) from the invert to the spring line. Circle 2 forms the sides, and Circle 3 forms the arch. Relative dimensions of each component of these egg-shaped sewers are provided in Table 1.

TABLE 1: Relative Component Dimensions of Cleveland Egg-Shaped Sewers

Component	No. 2		No. 3	
	Diameter	Depth	Diameter	Depth
Circle 1	$D_1 = 2R_i$	$d_1 = d$	$D_1 = 2R_i$	$d_1 = d$
Circle 2	$D_2 = 4R_i$	$d_2 = d + R_i \left(1 - \frac{1}{\sqrt{2}}\right)$	$D_2 = \frac{16}{3}R_i$	$d_2 = d + \frac{5}{3}R_i \left(1 - \frac{1}{\sqrt{2}}\right)$
Circle 3	$D_3 = 2R_i \left(2 - \frac{1}{\sqrt{2}}\right)$	$d_3 = d - R_i \left(\frac{2}{\sqrt{2}} - 1\right)$	$D_3 = \frac{2}{3}R_i \left(8 - \frac{5}{\sqrt{2}}\right)$	$d_3 = d - \frac{5}{3}R_i \left(\frac{2}{\sqrt{2}} - 1\right)$
Egg	$D_T = 2R_i \left(2 - \frac{1}{\sqrt{2}}\right)$	$d_s = R_i \left(1 + \frac{1}{\sqrt{2}}\right)$	$D_T = \frac{2}{3}R_i \left(8 - \frac{5}{\sqrt{2}}\right)$	$d_s = R_i \left(1 + \frac{5}{3\sqrt{2}}\right)$
	$D_V = 3R_i$		$D_V = \frac{11}{3}R_i$	

The diameter (D_1, D_2, D_3) of each component circle is derived relative to R_i as specified in engineering drawings from the City of Cleveland, and the flow depth in each component circle (d_1, d_2, d_3) is derived relative to the flow depth (d) in the No. 2 and No. 3 Cleveland egg-shaped sewers.²

Historical Perspective

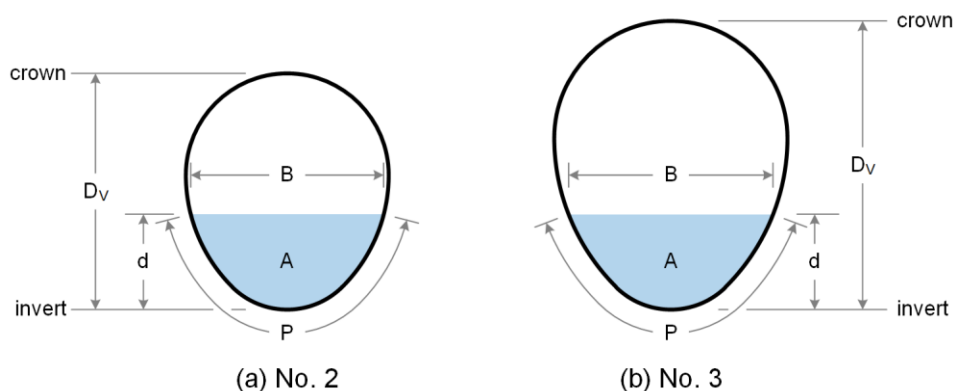
The egg-shaped sewer was developed in the 19th Century to enhance self-cleansing in combined sewers by channeling wastewater flows through a smaller cross-section during low flow conditions, resulting in a greater flow velocity when compared to a similarly sized circular sewer.³ John Phillips (1817 – 1897) is associated with several egg-shaped sewer designs used in London, two of which became most popular.⁴ These designs spread throughout the world and were adopted in many developing cities, including Cleveland, Ohio.⁵

While these egg-shaped sewers were successfully introduced in other cities, structural problems were encountered in Cleveland due to groundwater and unfavorable soil conditions.⁵ Cyrus G. Force, Jr. (1841 – 1922), an engineer who worked for the City of Cleveland, designed an egg-shaped sewer section to overcome these difficulties and proposed several sizes designated No. 1 through No. 14.^{5,6} The No. 1 Cleveland egg-shaped sewer was never adopted, and other egg-shaped sewer sections were implemented for No. 2 and No. 3 Cleveland egg-shaped sewers, designed by others.^{5,7,8} No. 4 through No. 16 Cleveland egg-shaped sewers were adopted as designed by Cyrus G. Force, Jr. and were eventually extended to additional sizes, including No. 17 through No. 20 Cleveland egg-shaped sewers.² While unique to the City of Cleveland, these sewers have passed the test of time, with many of them in service for well over 100 years.

Geometric Elements

Several *geometric elements* are needed for engineering calculations involving sewers flowing partially full and are a function of flow depth (d), as well as the size and shape of the sewer cross section. The *wetted area* (A) is the part of the sewer cross section occupied by the wastewater flow, while the *wetted perimeter* (P) is the part of the sewer perimeter in contact with the wastewater flow.⁹ The *surface width* (B) is the width of the flow surface.⁹ The geometric elements of No. 2 and No. 3 Cleveland egg-shaped sewers are illustrated in Figure 3.

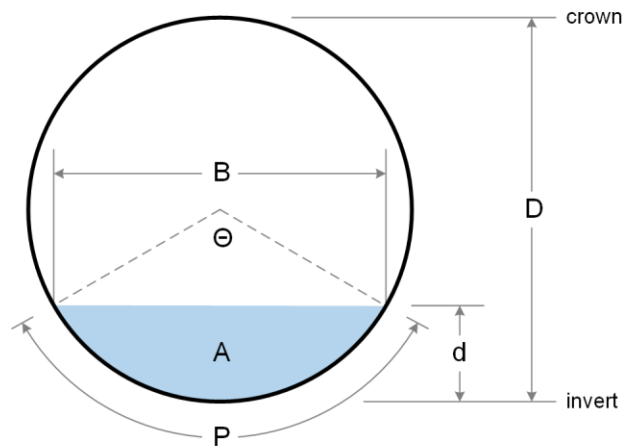
FIGURE 3: Geometric Elements of Partially Filled Cleveland Egg-Shaped Sewers



Partially Filled Circular Sewer

Since an egg-shaped sewer is constructed from several circles, its geometric elements are based on the geometry of a partially filled circular sewer as illustrated in Figure 4 and defined in Equations (1) through (4).⁹

FIGURE 4: Geometric Elements of a Partially Filled Circle



$$\theta = 2 \cos^{-1} \left(1 - 2 \frac{d}{D} \right) \quad (1)$$

$$A = \frac{D^2}{8} (\theta - \sin \theta) \quad (2)$$

$$P = \frac{D}{2} \theta \quad (3)$$

$$B = D \sin \frac{\theta}{2} \quad (4)$$

where: θ = central angle, radians
 d = flow depth, ft
 D = diameter, ft
 A = wetted area, ft²
 P = wetted perimeter, ft
 B = surface width, ft

Partially Filled Cleveland Egg-Shaped Sewer – No. 2

Once the geometry of the No. 2 Cleveland egg-shaped sewer is defined, several regions are identified with distinct geometric calculations. Three regions within the No. 2 Cleveland egg-shaped sewer are detailed in Table 2.

TABLE 2: Geometric Regions of the Cleveland Egg-Shaped Sewer – No. 2

Region	Depth
I	$0 \leq d \leq R_i \left(1 - \frac{1}{\sqrt{2}}\right)$
II	$R_i \left(1 - \frac{1}{\sqrt{2}}\right) < d \leq R_i \left(1 + \frac{1}{\sqrt{2}}\right)$
III	$R_i \left(1 + \frac{1}{\sqrt{2}}\right) < d \leq 3R_i$

Geometric elements in Region I are based on Circle 1. Geometric elements in Region II are based on Circle 1 and Circle 2, and geometric elements in Region III are based on Circle 1, Circle 2, and Circle 3.

The wetted area of a partially filled No. 2 Cleveland egg-shaped sewer is calculated using the compound equation shown in Equation (5).

$$A_{egg} = \quad (5)$$

$+A_1$ where $d = d$	$+A_2$ where $d = d$ $-A_2$ where $d = R_i \left(1 - \frac{1}{\sqrt{2}}\right)$ $-\frac{2R_i}{\sqrt{2}} \left[d - R_i \left(1 - \frac{1}{\sqrt{2}}\right) \right]$ where $d = d$ $+A_1$ where $d = R_i \left(1 - \frac{1}{\sqrt{2}}\right)$	$+A_3$ where $d = d$ $-A_3$ where $d = R_i \left(1 + \frac{1}{\sqrt{2}}\right)$ $+A_2$ where $d = R_i \left(1 + \frac{1}{\sqrt{2}}\right)$ $-A_2$ where $d = R_i \left(1 - \frac{1}{\sqrt{2}}\right)$ $-2R_i^2$ $+A_1$ where $d = R_i \left(1 - \frac{1}{\sqrt{2}}\right)$
when d is in Region I	when d is in Region II	when d is in Region III
Circle 1 $\theta_1 = 2 \cos^{-1} \left(1 - \frac{d}{R_i}\right)$ $A_1 = \frac{R_i^2}{2} (\theta_1 - \sin \theta_1)$	Circle 2 $\theta_2 = 2 \cos^{-1} \left[1 - \frac{d\sqrt{2} + R_i(\sqrt{2} - 1)}{2R_i\sqrt{2}} \right]$ $A_2 = 2R_i^2 (\theta_2 - \sin \theta_2)$	Circle 3 $\theta_3 = 2 \cos^{-1} \left[1 - \frac{d\sqrt{2} - R_i(2 - \sqrt{2})}{R_i(2\sqrt{2} - 1)} \right]$ $A_3 = \frac{R_i^2 (9\sqrt{2} - 8)}{4\sqrt{2}} (\theta_3 - \sin \theta_3)$

The wetted area and wetted perimeter of a No. 2 Cleveland egg-shaped sewer *when flowing full* are calculated using Equation (8) and Equation (9), respectively.

$$A_{egg} = R_i^2 \left[\pi \left(\frac{7}{2} - \frac{2}{\sqrt{2}} \right) - \frac{1}{2} \right] \quad (8)$$

$$P_{egg} = \pi R_i \left(\frac{7}{2} - \frac{1}{\sqrt{2}} \right) \quad (9)$$

where: A_{egg} = wetted area, ft²
 P_{egg} = wetted perimeter, ft
 R_i = invert radius, ft

These equations represent special cases of Equation (5) and Equation (6) under full-pipe flow conditions.

The wetted perimeter of a partially filled No. 3 Cleveland egg-shaped sewer is calculated using the compound equation shown in Equation (11).

$$P_{egg} = \quad (11)$$

$+P_1$ where $d = d$ <i>when d is in Region I</i>	$+P_2$ where $d = d$ $-P_2$ where $d = R_i \left(1 - \frac{1}{\sqrt{2}}\right)$ $+P_1$ where $d = R_i \left(1 - \frac{1}{\sqrt{2}}\right)$ <i>when d is in Region II</i>	$+P_3$ where $d = d$ $-P_3$ where $d = R_i \left(1 + \frac{5}{3\sqrt{2}}\right)$ $+P_2$ where $d = R_i \left(1 + \frac{5}{3\sqrt{2}}\right)$ $-P_2$ where $d = R_i \left(1 - \frac{1}{\sqrt{2}}\right)$ $+P_1$ where $d = R_i \left(1 - \frac{1}{\sqrt{2}}\right)$ <i>when d is in Region III</i>
Circle 1	Circle 2	Circle 3
$\theta_1 = 2 \cos^{-1} \left(1 - \frac{d}{R_i}\right)$ $P_1 = R_i \theta_1$	$\theta_2 = 2 \cos^{-1} \left[1 - \frac{3d\sqrt{2} + 5R_i(\sqrt{2} - 1)}{8R_i\sqrt{2}}\right]$ $P_2 = \frac{8}{3} R_i \theta_2$	$\theta_3 = 2 \cos^{-1} \left[1 - \frac{3d\sqrt{2} - 5R_i(2 - \sqrt{2})}{R_i(8\sqrt{2} - 5)}\right]$ $P_3 = \frac{1}{3} R_i \left(8 - \frac{5}{\sqrt{2}}\right) \theta_3$

The surface width of a partially filled No. 3 Cleveland egg-shaped sewer is calculated using the compound equation shown in Equation (12).

$$B_{egg} = \quad (12)$$

$+B_1$ where $d = d$ <i>when d is in Region I</i>	$+B_2$ where $d = d$ $-\frac{10}{3\sqrt{2}} R_i$ <i>when d is in Region II</i>	$+B_3$ where $d = d$ <i>when d is in Region III</i>
Circle 1	Circle 2	Circle 3
$\theta_1 = 2 \cos^{-1} \left(1 - \frac{d}{R_i}\right)$ $B_1 = 2R_i \sin \frac{\theta_1}{2}$	$\theta_2 = 2 \cos^{-1} \left[1 - \frac{3d\sqrt{2} + 5R_i(\sqrt{2} - 1)}{8R_i\sqrt{2}}\right]$ $B_2 = \frac{16}{3} R_i \sin \frac{\theta_2}{2}$	$\theta_3 = 2 \cos^{-1} \left[1 - \frac{3d\sqrt{2} - 5R_i(2 - \sqrt{2})}{R_i(8\sqrt{2} - 5)}\right]$ $B_3 = \frac{2}{3} R_i \left(8 - \frac{5}{\sqrt{2}}\right) \sin \frac{\theta_3}{2}$

The wetted area and wetted perimeter of a No. 3 Cleveland egg-shaped sewer *when flowing full* are calculated using Equation (13) and Equation (14), respectively.

$$A_{egg} = R_i^2 \left[\frac{\pi}{18} \left(113 - \frac{80}{\sqrt{2}} \right) - \frac{25}{18} \right] \quad (13)$$

$$P_{egg} = \pi R_i \left(\frac{9}{2} - \frac{5}{3\sqrt{2}} \right) \quad (14)$$

where: A_{egg} = wetted area, ft²
 P_{egg} = wetted perimeter, ft
 R_i = invert radius, ft

These equations represent special cases of Equation (10) and Equation (11) under full-pipe flow conditions.

Designated Sizes of Cleveland Egg-Shaped Sewers

No. 2 and No. 3 Cleveland egg-shaped sewers designed and constructed in Cleveland, Ohio have a designated invert radius (R_i) of 9 inches. Based on this designation, the dimensions of these sewers are shown in Table 4.

TABLE 4: Dimensions of Cleveland Egg-Shaped Sewers

No. N	R_i (ft)	D_T (ft)	D_V (ft)	d_s (ft)	A_{egg} (ft ²)	P_{egg} (ft)
2	0.7500	1.9393	2.2500	1.2803	3.4046	6.5806
3	0.7500	2.2322	2.7500	1.6339	4.7589	7.8261

Validation

Equations (5) through (7) are validated by computing the wetted area, wetted perimeter, and surface width at various flow depths for a No. 2 Cleveland egg-shaped sewer with a specified invert radius (R_i) and comparing the results to reference sources and/or values derived from them. Results are provided in Table 5 for a No. 2 Cleveland egg-shaped sewer where $R_i = 9$ inches. The flow depths chosen for comparison include the maximum flow depth in Regions I, II, and III.

TABLE 5: Validation of Equations for a Partially Filled Cleveland Egg-Shaped Sewer – No. 2

Depth	Wetted Area			Wetted Perimeter			Surface Width		
	Eqn. (5)	Ref.	Δ	Eqn. (6)	Ref.	Δ	Eqn. (7)	Ref.	Δ
	(ft ²)	(ft ²)	(%)	(ft)	(ft)	(%)	(ft)	(ft)	(%)
I	0.1605	0.1605	0.0%	1.1781	1.1781	0.0%	1.0607	1.0607	0.0%
II	1.9277	1.9277	0.0%	3.5343	3.5343	0.0%	1.9393	1.9393	0.0%
III	3.4046	3.4046	0.0%	6.5806	6.5806	0.0%	0.0000	0.0000	0.0%

Equations (10) through (12) are validated by computing the wetted area, wetted perimeter, and surface width at various flow depths for a No. 3 Cleveland egg-shaped sewer with a specified invert radius (R_i) and comparing the results to reference sources and/or values derived from them. Results are provided in Table 6 for a No. 3 Cleveland egg-shaped sewer where $R_i = 9$ inches. The flow depths chosen for comparison include the maximum flow depth in Regions I, II, and III.

TABLE 6: Validation of Equations for a Partially Filled Cleveland Egg-Shaped Sewer – No. 3

Depth	Wetted Area			Wetted Perimeter			Surface Width		
	Eqn. (10)	Ref.	Δ	Eqn. (11)	Ref.	Δ	Eqn. (12)	Ref.	Δ
	(ft ²)	(ft ²)	(%)	(ft)	(ft)	(%)	(ft)	(ft)	(%)
I	0.1605	0.1605	0.0%	1.1781	1.1781	0.0%	1.0607	1.0607	0.0%
II	2.8021	2.8021	0.0%	4.3197	4.3197	0.0%	2.2322	2.2322	0.0%
III	4.7589	4.7589	0.0%	7.8261	7.8261	0.0%	0.0000	0.0000	0.0%

At the maximum flow depth in Region I, the wetted area, wetted perimeter, and surface width are equivalent to those of Circle 1 at the specified flow depth. The values obtained from Equations (5) through (7) for a No. 2 Cleveland egg-shaped sewer and Equations (10) through (12) for a No. 3 Cleveland egg-shaped sewer equal the expected values, as shown in Table 5 and Table 6, respectively.

At the maximum flow depth in Region II, no reference equations are available for comparison. However, the expected wetted area and wetted perimeter for a No. 2 Cleveland egg-shaped sewer is derived by taking the full-pipe values from Equations (8) and (9) and subtracting the wetted area or wetted perimeter of Circle 3 when 50% full, and the expected wetted area and wetted perimeter for a No. 3 Cleveland egg-shaped sewer

is derived by taking the full-pipe values from Equations (13) and (14) and subtracting the wetted area or wetted perimeter of Circle 3 when 50% full. While no reference equations is available for the surface width, the geometry of No. 2 and No. 3 Cleveland egg-shaped sewers dictates that it is equal to the transverse diameter at this flow depth. The values obtained from Equations (5) through (7) for a No. 2 Cleveland egg-shaped sewer and Equations (10) through (12) for a No. 3 Cleveland egg-shaped sewer equal these derived values and geometric expectations, as shown in Table 5 and Table 6, respectively.

At the maximum flow depth in Region III, Equations (8) and (9) are used to calculate the wetted area and wetted perimeter of a No. 2 Cleveland egg-shaped sewer under full-flow conditions, and Equations (13) and (14) are used to calculate the wetted area and wetted perimeter of a No. 3 Cleveland egg-shaped sewer. While no reference equations are available for the surface width, the geometry of No. 2 and No. 3 Cleveland egg-shaped sewers dictates that it is zero at this flow depth. The values obtained from Equations (5) through (7) for a No. 2 Cleveland egg-shaped sewer and Equations (10) through (12) for a No. 3 Cleveland egg-shaped sewer equal those obtained using reference equations and geometric expectations, as shown in Table 5 and Table 6, respectively.

Hydraulic Elements

Once the geometric elements of a partially filled Cleveland egg-shaped sewer are known, several *hydraulic elements* needed for commonly used wastewater engineering calculations can be determined. The *hydraulic radius* (R) is calculated using Equation (15) and is defined as the ratio of the wetted area to the wetted perimeter.⁹

$$R = \frac{A}{P} \quad (15)$$

where: R = hydraulic radius, ft
 A = wetted area, ft²
 P = wetted perimeter, ft

The *hydraulic mean depth* (d_h) is calculated using Equation (16) and is defined as the ratio of the wetted area to the surface width.⁹

$$d_h = \frac{A}{B} \quad (16)$$

where: d_h = hydraulic mean depth, ft
 A = wetted area, ft²
 B = surface width, ft

The hydraulic radius is used in the Manning Equation as shown in Equations (17) and (18) to estimate the flow velocity (v) and flow rate (Q) under uniform flow conditions.¹

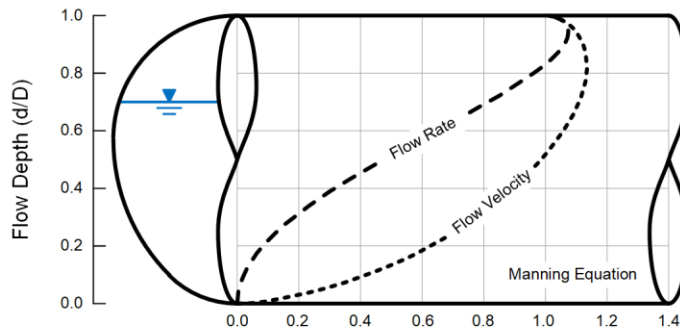
$$v = \frac{1.486}{n} R^{2/3} S^{1/2} \quad (17)$$

$$Q = \frac{1.486}{n} A R^{2/3} S^{1/2} \quad (18)$$

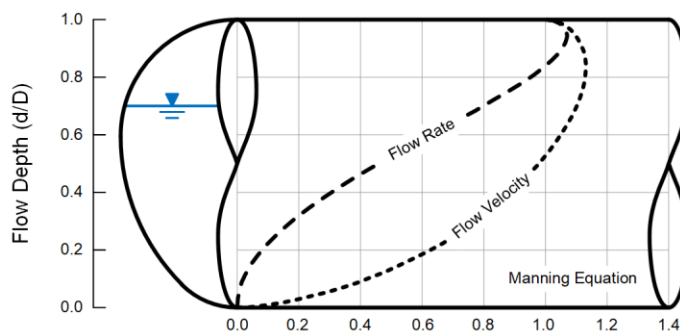
where: v = flow velocity, ft/s
 n = roughness coefficient
 R = hydraulic radius, ft
 S = slope of the energy gradient
 Q = flow rate, ft³/s
 A = wetted area, ft²

Hydraulic elements curves prepared using the Manning Equation for No. 2 and No. 3 Cleveland egg-shaped sewers at various relative flow depths are shown in Figures 5(a) and 5(b), respectively.

FIGURE 5: Hydraulic Elements of Cleveland Egg-Shaped Sewers



(a) No. 2 Flow Velocity (v/v_D), Flow Rate (Q/Q_D)



(b) No. 3 Flow Velocity (v/v_D), Flow Rate (Q/Q_D)

Other important properties enabled once the geometric elements of partially full Cleveland egg-shaped sewers are known include the Froude Number, Reynolds Number, and shear stress.^{9,10}

Conclusion

Combined sewers are designed and constructed with a wide variety of sewer cross sections. While the circular section is most common, other non-circular sections have also been used over the years. Working with combined sewers requires an understanding of the geometric and hydraulic elements of these non-circular sections when encountered.

The geometric elements of No. 2 and No. 3 Cleveland egg-shaped sewers flowing partially full have been defined, and equations for the wetted area, wetted perimeter, and surface width are provided and validated. The result is a concise reference for wastewater professionals working with egg-shaped sewers in combined sewers located in Cleveland, Ohio.

Symbols and Notation

The following symbols and notation are used in this paper:

VARIABLES

θ	= central angle, radians
d	= flow depth, ft
D	= diameter, ft
A	= wetted area, ft ²
P	= wetted perimeter, ft
B	= surface width, ft
R	= radius, ft
v	= flow velocity, ft/s
Q	= flow rate, ft ³ /s
n	= roughness coefficient
S	= slope of the energy gradient

SUBSCRIPTS

T	= transverse
V	= vertical
S	= spring line
1	= Circle 1
2	= Circle 2
3	= Circle 3
i	= invert
egg	= egg
h	= hydraulic

Acknowledgement

The author acknowledges Cyrus G. Force, Jr. and his colleagues whose engineering creativity in the late 1800s led to the design and construction of these egg-shaped sewers unique to Cleveland, Ohio. That they accomplished these designs with a more rudimentary knowledge of sewer hydraulics known at the time and with computational tools available in their day is astounding. Special thanks are extended to the Northeast Ohio Regional Sewer District (NEORS) who maintains many of these egg-shaped sewers to this day, as well as to the dedicated team at ADS Environmental Services who monitor flows within them and whose efforts were the inspiration for this work.

References

1. Metcalf & Eddy, Inc. (1981). *Wastewater Engineering: Collection and Pumping of Wastewater*. McGraw-Hill, New York, NY.
2. DeVaul, R.E. (2008). "Standard Plan for Egg Shaped Sewers – Dimensions and Areas," *Division of Engineering and Construction – Standard Construction Drawings*, File No. 73 M, Page 24.
3. Latham, B. (1878). *Sanitary Engineering: A Guide to the Construction of Works of Sewerage and House Drainage*, 2nd Edition. E & FN Spon, London.
4. Enfinger, K.L. (2024). "Working with Combined Sewers – Geometric and Hydraulic Elements of Egg-Shaped Sewers," *Proceedings of the Utility Engineering & Surveying Institute Pipelines Conference*; Calgary, AB; American Society of Civil Engineers: Reston, VA.
5. Force, Jr. C.G. (1880). "Design and Construction Table for Egg-Shaped Sewers," *Transactions of the American Society of Civil Engineers*, Volume 9, Issue 1, Pages 202-205.
6. Hoffmann, R. (1922). "Memoirs of Deceased Members: Cyrus Gildersleeve Force, Jr.," *Proceedings of the American Society of Civil Engineers*, Volume 68, Number 8, Pages 1729-1730.
7. Parmley, W.C. (1898). "Rainfall and Run-Off in Relation to Sewerage Problems," *Journal of the Association of Engineering Societies*, Volume XX, No. 3, Pages 204-225.
8. Parmley, W.C. (1900). "Sewer Maintenance," *Journal of the Association of Engineering Societies*, Volume XXIV, No. 6, Pages 370-383.
9. Butler, D., Digman, C., Makropoulos, C., and Davies, J.W. (2018). *Urban Drainage*, 4th Edition. CRC Press, Boca Raton, FL.
10. Enfinger, K.L. and Mitchell, P.S. (2010). "Scattergraph Principles and Practice – Evaluating Self-Cleansing in Existing Sewers Using the Tractive Force Method," *Proceedings of the World Environmental & Water Resources Congress 2010*: Providence, RI; American Society of Civil Engineers: Reston, VA.